Shell evolution beyond $Z = 28$ and $N = 50$: Spectroscopy of $^{81,82,83,84}$Zn


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Technological advances at radioactive beam facilities have provided the means to access extremely neutron-rich regions of the nuclear chart. Studies performed in these regions have illuminated interesting phenomena that cannot be described within the traditional shell model framework. Weakening of the shell-gaps at the conventional magic numbers and emergence of new magic numbers have been observed and predicted in hard-to-reach neutron-rich nuclei. Examples include: the disappearance of the N = 20 [1] and N = 28 [2–4] shell-gaps and the appearance of new magic numbers at N = 32 [5,6] and N = 34 [7].

Current radioactive beam intensities have facilitated even the more recent studies into the N = 50 magic number around 78Ni (Z = 28). 78Ni has garnered a lot of attention in recent experimental and theoretical investigations [8–14]. Highlights include the predicted inversion of the πp3/2 and πF5/2 orbitals in the 78Ni region [15], a prediction which was subsequently observed in 72Cu via measurements of the ground state magnetic moment and spin [16]. Theoretical work in the region predicts the 78Ni nucleus to have around 75% closed shell configuration [14,13] – more than for the doubly-magic 50Ni (N = 28) which was calculated to have 50–60% closed-shell configuration [17,14]. While recent theoretical calculations have predicted 78Ni to be doubly magic [18] a well-deformed prolate band is also suggested at low excitation energy [19].

The robustness of the shell closures at 78Ni have nuclear structure consequences in the region beyond N = 50. However, experimental data are limited due to difficulties in accessing these extremely exotic nuclei. As neutron-rich nuclei become accessible, one of the first measurements that can be made to probe the underlying structure is the spectroscopy of low-lying excited states. The E(2ν), E(4ν), and their ratio R_{4/2} = E(4ν) / E(2ν) provide a measure of the collectivity, where a low E(2ν) and high R_{4/2} are a signature of increased collectivity [20]. Presented in this letter are the spectroscopy measurements of low-lying states in 81,82,83,84Zn (Z = 30), of which 82,84Zn are the first two even–even nuclei north–east of 78Ni.

The experimental campaigns were conducted at the Radioactive Isotope Beam Factory (RIBF), operated jointly by the RIKEN Nishina Center and the Center for Nuclear Study of the University of Tokyo. A 238U primary beam was accelerated to 345 MeV/nucleon and subsequently impinged onto a 3 mm thick 9Be production target at the entrance of the BigRIPS separator [21]. Secondary beams of interest from the in-flight fission were then selected within BigRIPS using the B_ρ – ∆E – B_ρ technique. The second primary beam settings discussed in this work were centered on 75Cu and 85Ga in the first (2014) and second (2015) campaigns, respectively. Identification of beam ions was performed on an event-by-event basis in BigRIPS by measuring: energy loss in ionization chambers, time of flight, and the magnetic rigidity, B_ρ [22].

The experimental setup [23,24] used in the experiments consisted of the DALI2 high-efficiency gamma-ray spectrometer [25] and the MINOS device [26], a liquid hydrogen target surrounded by a time projection chamber (TPC). In the 2015 campaign secondary beams were incident on the 99(1) mm thick liquid hydrogen (secondary) target with energies of ~270 MeV per nucleon, and intensities measured to be 10, 125, 7, and 371 s⁻¹ for 83,84,85Ga, and 86Ge, respectively, over ~24 hours. In the 2014 campaign the liquid hydrogen target was 102(1) mm thick, and secondary beams were incident on the target with energies of ~250 MeV per nucleon and intensity measured to be 2 s⁻¹ for 82Ga over ~137 hours. The results presented here are from the second campaign, with the exception of the 82Ga(p, 2p)81Zn reaction which was measured in the first campaign [27]. Following MINOS, the reaction products were identified within the ZeroDegree spectrometer [21] using the same technique as in BigRIPS. Secondary residues were primarily produced in the (p, 2p) knockout reactions induced by the hydrogen of the MINOS target. Residual nuclei were also populated in multi-nucleon knockout reactions. The trajectories of the outgoing protons were tracked by the TPC of MINOS. The resulting tracks were used to reconstruct the vertex position, resulting in an improved Doppler correction. Surrounding MINOS was the DALI2 array, composed of 186 NaI scintillator detectors configured to accommodate the MINOS TPC. The full-energy peak detection efficiency of the setup was simulated within the GEANT4 framework [28] to be 35% for 500 keV γ rays emitted in flight from nuclei with an energy of 250 MeV/nucleon. DALI2 was energy calibrated using 60Co, 68V, and 137Cs gamma-ray sources. Calibration peaks from 662–1332 keV were used to obtain an energy uncertainty of 2 keV and energy resolution of 60 keV Full Width at Half Maximum (FWHM) at 662 keV, for a γ-ray source at rest, consistent with [29].

The γ-ray spectra were Doppler corrected using the reconstituted reaction vertex information obtained from MINOS. The GEANT4 toolkit [28] was used to simulate the response of DALI2 for individual transitions. The transition energies were determined by fitting the combination of simulated response functions and a two-exponential background to the spectra. If a decaying state has a long half-life it can cause a shifted γ-ray energy and broadened peak to be observed for the transition. Therefore, half-lives, t_{1/2}, of ~50 ps were considered in the simulations for the 2+ states in 82–84Zn, in good agreement with theoretical calculations, systematic trends in the immediate region of the nuclear chart, and the measured width of the transitions. The 4+ states were considered to be shorter lived with a half-life of ~15 ps. For example, a 618 (692) keV transition from a state with 50 (15) ps half-life yields an offset of 13 (6) keV due to the considered half-life alone. These uncertainties in the half-life form the largest component in
the quoted errors for the transition and are added in quadrature to the uncertainties in the energy calibration and the fit.

\(^{81}\text{Zn}\): \(^{81}\text{Zn}\) was produced from the \(^{82}\text{Ga}\)(p, 2p)\(^{81}\text{Zn}\) reaction channel. The \(\gamma\)-ray spectrum observed in this reaction is shown in Fig. 1(a). A strong transition was observed at 938(13) keV along with a tentative transition at 1235(17) keV. The inset of Fig. 1(a) suggests that the two transitions are not in coincidence. The 938 keV transition was observed in 13(3)% of the (p, 2p) reactions, while the 1235 keV transition was seen in 6(2)%.

\(^{82}\text{Zn}\): \(^{82}\text{Zn}\) was populated in the \(^{83}\text{Ga}\)(p, 2p)\(^{82}\text{Zn}\) reaction and the high statistics \(^{84}\text{Ga}\)(p, 2pn)\(^{82}\text{Zn}\) reaction. The \(\gamma\)-ray spectra for the two reactions are shown in Fig. 1(b) and 1(c). In both reaction channels a structure is observed at \(\sim 615\) keV with a deformed high-energy side of the peak. The insets in Fig. 1(b) and 1(c) show that the low- and high-energy sides of the main peak are coincident. Therefore, the wide peak in Fig. 1(b) and 1(c) is concluded to be a doublet, composed of a higher intensity 618(15) keV transition and a coincident 692(12) keV transition. An additional transition in \(^{82}\text{Zn}\) is observed in the (p, 2p) reaction channel spectrum, Fig. 1(b), at 369(17) keV. The first \(\gamma\)-ray spectroscopy of \(^{82}\text{Zn}\) was recently performed at the RIBF by Y. Shiga et al. [30]. They observed a 621(11) keV transition in the \(^{9}\text{Be}\)(X, \(^{82}\text{Zn}\) + \(\gamma\)) nucleon knockout reaction which was assigned as the \((2^+_1) \rightarrow 0^+_2\) transition. The 618(15) keV transition observed in this work is in excellent agreement with the previous work. The population ratios obtained in the (p, 2p) reaction are: 20(4)% 369(17) keV, 49(8)% 618(15) keV, and 28(5)% 692(12) keV.

\(^{83}\text{Zn}\): \(^{83}\text{Zn}\) was measured in the (p, 2p), (p, 2pn), (p, 3p), and (p, 3pn) channels, with the majority of the statistics observed in the \(^{86}\text{Ge}\)(p, 3pn)\(^{83}\text{Zn}\) reaction which is shown in Fig. 1(d). Two transitions are observed at 568(27) keV and 872(36) keV. The inset of Fig. 1(d) implies that the two transitions are not coincident.

\(^{84}\text{Zn}\): \(^{84}\text{Zn}\) was populated in the dedicated \(^{85}\text{Ga}\) setting. The \(^{84}\text{Zn}\) \(\gamma\)-ray spectrum (Fig. 1(e)) for the \(^{85}\text{Ga}\)(p, 2p)\(^{84}\text{Zn}\) reaction channel shows a clear transition at 599(20) keV. A weaker transition is also visible at 845(21) keV in the spectrum. Despite the limited statistics the two transitions are seen to be coincident in the insets of Fig. 1(e). The population ratios are: 38(7)% 599(20) keV and 11(3)% 845(21) keV.

To further understand the shell evolution in the zinc isotopes, three different state-of-the-art shell model calculations were performed. The first calculation, Ni78-II, utilised a model space outside an inert \(^{78}\text{Ni}\) core, whereas the second calculation, A3DA-m, used the full pf-shell and the \(g_9/2\) and \(d_{5/2}\) orbitals. The final calculation, PFSGU-U, assumes an inert \(^{60}\text{Ca}\) with a large valence space.

**Ni78-II Calculations**: These calculations were performed in the model space outside the \(^{78}\text{Ni}\) core, employing \(Z = 28–50\) \(\pi (f_{5/2},\) \(p_{3/2},\) \(p_{1/2},\) \(g_{9/2}\) and \(N = 50–82\) \(v (d_{5/2}, s_{1/2}, d_{3/2}, g_{7/2}, h_{11/2}\)) orbitals. Ni78-II calculations, established in Refs. [31–34], have previously been utilised successfully for \(^{83}\text{Br}\) [33], \(^{84,86}\text{Se}\) [32,34], and \(N = 52\) isotones [35] in the region north–east of \(^{78}\text{Ni}\).

**A3DA-m Calculations**: Monte Carlo Shell Model calculations [14] were performed using the A3DA-m interaction with a model space utilising the full pf shell, \(g_{9/2}\), and \(d_{5/2}\) orbitals for both protons and neutrons. A3DA-m calculations were previously compared to a number of isotopes in the region around \(^{78}\text{Ni}\) [14,36,37], including \(^{82}\text{Zn}\) [30]. The differing model space of the A3DA-m calculations permits \(^{78}\text{Ni}\) core-breaking configurations, in contrast to

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**Fig. 1.** Doppler-shift corrected \(\gamma\)-ray spectra from the (a) \(^{82}\text{Ga}(p,2p)^{81}\text{Zn}\), (b) \(^{83}\text{Ga}(p,2p)^{82}\text{Zn}\), (c) \(^{84}\text{Ga}(p,2pn)^{82}\text{Zn}\), (d) \(^{86}\text{Ge}(p,3pn)^{83}\text{Zn}\), and (e) \(^{85}\text{Ga}(p,2p)^{84}\text{Zn}\) reactions. The insets show examples of \(\gamma\)-\(\gamma\) coincidence analysis (not background subtracted), with vertical dashed-lines (red) indicating the gate energy, \(\gamma\)-\(\gamma\) multiplicity, \(M_\gamma\), conditions are indicated by the labels. The fits shown (black) are the combination of simulated response functions (red) and a two-exponential background (blue). (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)
the Ni78-II calculations. However, the A3DA-m model space above \( Z, N = 50 \) is limited to only the \( d_{5/2} \) orbital.

**PFSGD-U Calculations:** The final calculation has a model space that covers the full pf shell for protons and the full sdg shell for neutrons. PFSGD-U calculations were recently compared to Ni isotopes up to \(^{86}\text{Ni}\) \cite{19}. The PFSGD-U calculations use an inert core of \(^{40}\text{Ca}\), with valence orbitals up to \( Z = 40, N = 70 \). Therefore, the PFSGD-U calculation benefits from both \(^{78}\text{Ni}\) core-breaking and additional orbitals above \( N = 50 \).

The character of the Zn nuclei populated via proton knockout reactions can be described by the configuration of the Ga beam nucleus with a proton removed. Valence protons in the Ga ground states can be in both \( f_{5/2} \) and \( p_{3/2} \) orbitals. The A3DA-m calculation predicts that the \( f_{5/2} \) occupancy is a factor of two larger than that of the \( p_{3/2} \). See Table 1 for a summary of the experimentally observed \( \gamma \)-ray transitions in \(^{82,84}\text{Zn}\) and the corresponding results of the three calculations.

\(^{81}\text{Zn}: \) Assuming a predominantly \((\pi f_{5/2})^3vd_{5/2}\) character of the \(^{82}\text{Zn}\) ground state, removing a proton would yield \(^{81}\text{Zn}\) low-lying states of \((\pi f_{5/2})^2vd_{5/2}\) character. Thus, the ground state \((\pi f_{5/2})^2_0vd_{5/2}\) and lowest excited states \((\pi f_{5/2})^2_2vd_{5/2}\) would be populated (note that the indicated configurations for the Zn isotopes have to be sizeable, but not necessarily dominant). The observed 938(13) and 1235(17) keV transitions most likely connect these \((\pi f_{5/2})^2vd_{5/2}\) states with the ground state, possibly via the low-lying \( 1/2^+ \) \( \pi s_{1/2} \) state. However, there is not enough information for definite spin-parity assignments.

\(^{82}\text{Zn}: \) \(^{82}\text{Zn}\) states populated in \((p,2p)\) reactions will have \((\pi f_{5/2})^2(vd_{5/2})^0_0\) and \((\pi p_{3/2})^2(vd_{5/2})^0_0\) configurations. The ground state is predicted to have \((\pi f_{5/2})^0_0\) character. Therefore we expect strong population of the \( 2_1^+ \) and \( 4_1^+ \) \((\pi f_{5/2})^2_0vd_{5/2}\) states as well as \( 0^+_2 \) and \( 2_2^+ \) states with \((\pi p_{3/2})^0_0\) character. Based on the intensities and coincidences we assign the 618(15) keV \( \gamma \)-ray to the \((2_1^+ \rightarrow 0^+_2)\) transition and the 692(12) keV to the \((4_1^+ \rightarrow 2_1^+)\). The 369(17) keV is rather tentatively assigned to the \((0^+_5 \rightarrow 2_1^+)\) transition with excellent agreement to the Ni78-II calculation, but quite far from the predictions of the other two. The Ni78-II calculation predicts the \( 2_1^+, 0^+_2, \) and \( 4_1^+ \) states \(~200\) keV higher than observed, but the relative spacing of these states is in excellent agreement with experiment. A3DA-m calculations provide good agreement to experiment, predicting the \( 2_1^+ \) state \(~100\) keV higher than observed while the \( 4_1^+ \) is within \( 10\) keV of the experimental energy. The PFSGD-U calculation yields an excellent agreement with the experimental \( 2_1^+ \) state, while the \( 4_1^+ \) and \( 0^+_2 \) states are predicted \(~100\) keV and \(~250\) keV higher in energy, respectively.

\(^{83}\text{Zn}: \) Low-lying \(^{83}\text{Zn}\) states are expected to have a configuration characterised by \((\pi f_{5/2})^2(vd_{5/2})^3\). A ground state with \((\pi f_{5/2})^2_0(vd_{5/2})^3\) character, and low-lying excited states with

<table>
<thead>
<tr>
<th>( J^\pi \rightarrow J^\pi )</th>
<th>( E_\gamma ) (keV)</th>
<th>( E_{\text{extr}} ) (keV)</th>
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<tbody>
<tr>
<td>( 2_1^+ \rightarrow 0^+_2 )</td>
<td>618(15)</td>
<td>621</td>
</tr>
<tr>
<td>( 4_1^+ \rightarrow 2_1^+ )</td>
<td>692(12)</td>
<td>798</td>
</tr>
<tr>
<td>( 0^+_2 \rightarrow 2_1^+ )</td>
<td>369(17)</td>
<td>731</td>
</tr>
<tr>
<td>( 2_1^+ \rightarrow 0^+_2 )</td>
<td>599(20)</td>
<td>552</td>
</tr>
<tr>
<td>( 4_1^+ \rightarrow 2_1^+ )</td>
<td>845(21)</td>
<td>727</td>
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\( \gamma \)-ray transitions energies in \(^{82,84}\text{Zn}\) compared to the results of the Ni78-II, A3DA-m, and PFSGD-U calculations.
The calculation. The A3DA-m calculations predict the Zn isotopes exactly. However, the PFSDG-U calculations over-predict the Zn isotopes, especially for lighter Zn isotopes. The agreement is improved from 51, 52, and 54 isotopes, respectively. A similar pattern is observed for N = 51 isotones, where the 3/2+ state with configuration (σ f5/2)2v d5/2 is over-predicted in zinc with the agreement improving at higher Z. These observations suggest that the low-lying states in nuclei closer to 78Ni have a significant contribution from core-breaking configurations. Allowing more collective contributions in the calculation should bring down the predicted energy of the states and provide a closer agreement to experiment.

Both the A3DA-m and PFSDG-U calculations predict the 78Ni core to be broken, but the PFSDG-U calculation has more valence orbitals above N = 50. Fig. 3 compares the Ni78-II, A3DA-m, and PFSDG-U calculations for the Zn chain. The inclusion of core-breaking in the A3DA-m calculations results in a better agreement of the 2+ in 82Zn. In 84Zn the agreement has worsened, with the A3DA-m predicting a similar 2+ energy as the Ni78-II. The A3DA-m calculations only consider the d5/2 orbital above N = 50, therefore as we approach N = 56 the role of higher orbitals becomes more significant and needs to be considered. The increasing discrepancy as we go from N = 52 to N = 54 demonstrates this. The major merit of A3DA-m calculation is the continuation from the lighter Zn isotopes, seen in Fig. 3, although the A3DA-m calculations are reaching a neutron-rich limit where the calculations suffer from the lack of valence neutron orbitals to complement the allowed core-breaking. While the PFSDG-U calculation benefits from both core breaking and a large valence space, which results in an improved agreement in the Zn systems (Fig. 3). The 2+ states in particular are reproduced extremely well by the PFSDG-U calculation.

A magic or semi-magic core can be distorted as valence nucleons are added to a closed shell. In the typical case of the well-known Sm isotopes [38], shape evolution is seen from a seniority level pattern in 144Sm82, to a vibrational pattern in 148Sm84, and finally a rotational one in 154Sm82. In this smooth change, 148Sm84 represents the transition between the seniority and vibrational schemes. In the case of Zn isotopes, with only two protons outside the Z = 28 (sub-)shell, the situation is different. As the present experimental results attest for the first time, the proton-neutron correlations are strong enough for a rapid change from the semi-magic structure at N = 50 to a collective structure at N = 52. This is ascribed partly to the weak Z = 28 super-magic structure, which is a consequence of the repulsive nature of the tensor force between the proton f7/2 and the fully occupied neutron g9/2 orbits [15,39]. On the other hand, the N = 50 closed shell structure is maintained rather well, as assumed in the Ni78-II calculation and also as shown in the A3DA-m calculations with the occupation number of the neutron g9/2 greater than 9.9. The PFSDG-U calculations also supports this conclusion.

In summary, new low-lying excited states in the neutron-rich 81, 82, 83, 84Zn isotopes have been investigated. These measurements included the first observation of the 4+ state in 82Zn and 2+ and 4+ states in 84Zn. The main conclusion is that the magicity is confined to N = 50 only. The experimental results were compared to three state-of-the-art shell-model calculations, which all correctly predict that this, and that the N = 52, 54 Zn isotopes exhibit collective-like character.

These comparisons reveal that breaking the 78Ni core provides a significant contribution to low-lying states beyond Z = 28 and N = 50. Current shell-model calculations need to be adapted to include sufficient valence orbitals above N = 50 while also allowing the 78Ni core to be broken. These findings show that core-breaking configurations provide a significant contribution to the structure of low-lying states in the vicinity of 78Ni. Recently, low-energy core-excited states were observed in 79Zn [40] and 80Ge [41] nuclei below N = 50. Shell-model developments that incorporate both a large neutron space and include core-breaking are necessary to understand the neutron-rich nuclei in the vicinity of 78Ni, in this theoretical framework. The recently developed PFSDG-U calculation [19] demonstrates the improved agreement obtained when considering both factors.

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