Shape Evolution in Neutron-rich Krypton Isotopes beyond $N = 60$ : First spectroscopy of $^{98,100}$Kr


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We report on the first $\gamma$-ray spectroscopy of low-lying states in neutron-rich $^{98,100}$Kr isotopes obtained from $^{99,101}$Rb(p,2p) reactions at $\sim 220$ MeV/nucleon. A reduction of the $2^+_1$ state energies beyond $N = 60$ demonstrates a significant increase of deformation, shifted in neutron number compared to the sharper transition observed in strontium and zirconium isotopes. State-of-the-art beyond-mean-field calculations using the Gogny D1S interaction predict level energies in good agreement with experimental results. The identification of a low-lying ($0^+_2$, $2^+_2$) state in $^{98}$Kr provides the first experimental evidence of a competing configuration at low energy in neutron-rich krypton isotopes consistent with the oblate-prolate shape coexistence picture suggested by theory.

Sudden variations of nuclear properties as a function of nucleon number lie at the heart of our understanding of atomic nuclei. The nuclear shell model was itself motivated by the discontinuities observed in two-nucleon separation energies and radii at specific (magic) nucleon numbers [1, 2]. Similarly, the presence of a rapid onset of deformation and change of equilibrium shape when adding only one or few nucleons drives the modeling of collectivity as it highlights the interplay between macroscopic properties and microscopic degrees of freedom. Related to the competition between the sphericity-favoring pairing interaction and the deformation-driving neutron-proton interaction [3], such a rapid growth of collectivity can be described in different frameworks. In the context of shape coexistence [4], an abrupt change of ground state properties can be interpreted as stemming from the crossing of two distinct quantum configurations of nucleons coexisting at low excitation energy. An intruder configuration, such as a multiparticle-multihole excitation above a closed shell or subshell, can for example profit from residual interactions with other nucleons to become energetically favorable. Another interpretation consists in describing this drastic shape change as a quantum phase transition [5], and transitional nuclei as critical points described using dynamical symmetries [6, 7]. The differences between these two mechanisms of shape change are subtle [8], and debates persist on the modeling of transitional regions [9, 10]. Across the nuclear chart, one of the most drastic and rapid shape transitions appears in the $A \simeq 100$ region at neutron number $N = 60$ for neutron-rich zirconium and strontium isotopes [4, 11]. The main experimen-
unaltered signatures for this shape change come from ground state properties, namely a discontinuity in binding energies [12] and an increase in charge radii [13], but also from the spectroscopy of low-lying $2^+_1$ states showing a sudden drop in energy [14]. In addition, the shape change is accompanied by the gradual lowering of an excited $0^+_1$ state [15, 16], interpreted as the band-head of a deformed configuration finally crossing with the spherical ground-state band at $N = 60$. As opposed to other regions of shape coexistence, all the detailed studies of transition amplitudes between low-lying states in $^{98}$Sr [17–19] and $^{100}$Zr [20–22] point to a weak mixing ($\leq 20\%$) between the two unperturbed configurations in the $0^+_1$ states, compatible with the picture of a sudden structural change. Recently, shape coexistence was also directly established away from the $N = 60$ transition in $^{94,96}$Zr [23, 24] pointing to a more widespread phenomenon in the region and to the importance of the $Z = 40$ sub-shell closure in this respect. More specifically, large-scale Monte Carlo shell model predictions [25] suggested that the deformed $0^+_1$ states in $^{98,100}$Zr isotopes arise from a sizeable excitation of protons to the $0g_{9/2}$ orbital across the $Z = 40$ sub-shell closure together with a close grouping of neutron effective single particle energies, both mediated by the tensor and central forces. Interestingly, the sudden onset of deformation at $N = 60$ in the zirconium and strontium chains was not observed for $^{96}$Kr [26]. Instead, a smooth reduction of $E(2^+_1)$ energy and the rise of $B(E2, 0^+_1 \rightarrow 2^+_1)$ excitation strength suggest a gradual development of collectivity. Moreover, no low-lying intruder states have been observed yet around $N = 60$ for krypton isotopes, i.e., no clear evidence of shape coexistence exists. Mass measurements of $^{96,98}$Kr [27], and $^{98,100}$Rb [28] isotopes together with charge radii studies [29, 30] also demonstrated that this abrupt $N = 60$ shape transition extends down to $Z = 37$ and not to $Z = 36$ in $^{96}$Kr. However, in the unexplored $N > 60$ region for krypton isotopes, one cannot exclude that a few additional neutrons could trigger a shape transition between prolate and oblate deformed configurations, predicted to compete at low excitation energies [28, 31–34]. In this letter, we present the spectroscopy of very neutron-rich $^{98,100}$Kr nuclei and characterize for the first time the evolution of collectivity beyond $N = 60$ in krypton isotopes.

The experiment was performed at the Radioactive Isotope Beam Factory at the RIKEN Nishina Center. The in-flight fission of a $^{238}$U beam with a mean intensity of 27 pA accelerated to 345 MeV/nucleon was induced by the collision with a 3-mm thick $^9$Be primary target at the object point of the BigRIPS separator [35]. Purification of the secondary beam was performed using Al degraders at the F1 and F5 dispersive planes (5 and 2-mm thick). The secondary cocktail beam containing 6.4% of $^{99}$Rb and 0.4% of $^{101}$Rb at respective averaged rates of 220 and 16 s$^{-1}$ impinged for 29 hours on a 99(1)-mm thick liquid hydrogen target of 73.22(8) kg/m$^3$ density cooled to 20 K. Event-by-event identification of projectiles and reaction residues in atomic number (Z) and mass-over-charge (A/Q) ratio was achieved using the TOF-$B_\rho$ method [35] in both BigRIPS and ZeroDegree spectrometers. Radioactive isotopes of $^{98,100}$Kr were produced via the (p,2p) direct reactions from $^{99,101}$Rb at energies ranging from $\sim$260 to $\sim$170 MeV/nucleon, respectively at the entrance and exit of the target.

The MINOS time projection chamber (TPC) [36] surrounding the target cell was used to reconstruct the reaction vertex position using the measured tracks of the outgoing protons. The reconstructed vertex was defined as the middle of the segment of closest approach between two trajectories: either from the two outgoing protons or from one proton and the beam particle tracked through two upstream position-sensitive parallel-plate avalanche counters (PPACs) [37]. The detection efficiency of at least one proton was simulated at 95% with a vertex position resolution of 5 mm (FWHM) along the beam axis [36]. The DAL12 high-efficiency gamma spectrometer [38] surrounded the MINOS device to detect in-flight de-excitation gamma-rays of $^{98,100}$Kr. It was composed of 186 NaI(Tl) crystals calibrated using $^{88}$Y, $^{60}$Co, $^{137}$Ba and $^{137}$Cs sources down to 356 keV. Add-back was applied when the centers of hit detectors were less than 15 cm apart. A full simulation of the array was per-
formed with the GEANT4 toolkit [39] to extract response functions. The simulations included: (i) individual crystal thresholds set at 100 keV on average, (ii) individual energy resolutions obtained using the calibration sources, (iii) experimental velocity distributions of projectiles from BigRIPS, and (iv) the lifetime of the decaying state. This simulation resulted in a full-energy peak detection efficiency of 41% for 500-keV γ-rays emitted in-flight along the target at relative velocity \( \beta = v/c \) ranging from 0.62 to 0.54. Other beam energy losses through materials along the line were taken into account for the beam velocity determination and benchmarked using an empty target measurement (relative agreement of 0.2%). Moreover, the full analysis procedure including Doppler correction and lifetime effects in the simulated response functions was validated on \(^{84}\)Kr for which the \( 2^+_1 \rightarrow 0^+_g \) transition energy was extracted with a 2 keV deviation from published values [26, 40], well within experimental uncertainties.

Doppler-corrected γ-ray spectra of \(^{98,100}\)Kr are presented in Fig. 1 together with least-squares fits including simulated response functions of identified transitions and a two-component exponential background. This background was folded with a step function to account for the low energy cutoff. Starting with \(^{98}\)Kr in Fig. 1(a), four peaks are visible on the energy spectrum and each one was fitted using a set of response functions assuming different energies and lifetimes. This procedure led to transition energies of 216(10), 329(7), 498(13) and 638(25) keV. Uncertainties are dominated by systematic errors from lifetime effects estimated using upper limits from \( \chi^2 \) profiles but also include a statistical contribution from the fit and a calibration error (4 keV) in the considered energy range. With respect to the 329-keV transition, the intensity of the 216-keV γ-ray extracted from the peak shape is significant but uncertain (between 50 and 120%) due to the ambiguity induced by the unknown shape of the low-energy background. Background-subtracted γ-γ coincidence spectra gated on the peaks corresponding to the 216 and 498-keV spectrum are shown in the inset of Fig. 1(a). These two transitions are in coincidence with the 329-keV transition but not between themselves. Based on these coincidences and in line with γ-ray intensities, the 329-keV transition was assigned to the \( 2^+_1 \rightarrow 0^+_g \) deexcitation with its two coincident γ-rays on top as shown in the proposed level scheme in Fig. 2(b). The weak 638-keV transition, enhanced in the \(^{100}\)Rb(p,2pn)\(^{88}\)Kr channel, was not seen in coincidence with any of the other γ-rays. Therefore, it may be a transition to the ground state as indicated in dashed line in Fig. 2(b).

For the 545-keV state, two spin-parity hypotheses are compatible with the non-observation of a transition to the ground state and with a 216-keV transition short-lived enough to be measured in this experiment: (i) either a \( 0^+_2 \) state with a large B(E2, \( 0^+_2 \rightarrow 2^+_1 \)) or (ii) a \( 2^+_2 \) state decaying via a M1-dominated transition to the \( 2^+_1 \) state. In addition, a \( 4^+_1 \) spin-parity has been discarded for this state because it would lead to a \( E(4^+_1)/E(2^+_1) \) ratio of \( \sim 1.6 \) typical of rigid spherical nuclei, very unlikely in such a mid-shell region. For the 827-keV state, a \( 4^+_1 \) tentative assignment is favored by this experiment based on the non-observation of a decay to the ground state and on relative intensities of the \( 4^+_1 \rightarrow 2^+_1 \) and \( 2^+_1 \rightarrow 0^+_g \) transitions populated by \((p,2p)\) reactions to other nuclei studied in the same conditions [41–43]. Following the same procedure for \(^{100}\)Kr (Fig. 1(b)), only one transition at 309(10) keV was observed and assigned to the \( 2^+_1 \rightarrow 0^+_g \) transition.

Our results extend the \( E(2^+_1) \) trend shown in Fig. 2(a) up to \( N = 64 \) for the krypton isotopes. While a rather flat behavior persisted up to \( N = 60 \) with previously measured values, our work indicates a significant drop in energy of 40% at \( N = 62 \) and a stabilization afterwards. Compared to Sr and Zr, the overall trend behaves more smoothly and a reduced but marked decrease in energy is shifted to \( N = 62 \). In addition, the identification of a \((0^+_2, 2^+_2)\) state at 545(17) keV in \(^{98}\)Kr close to the \( 2^+_1 \) state is the first experimental evidence for a coexisting band intruding at low energy in neutron-rich krypton isotopes. These observations point to structural changes around \( N = 62 \). Are they manifestations of an underlying shape transition somehow analogous to the ones observed in strontium and zirconium isotopes?

To gain insight into this subtle evolution, we used the 5-Dimensional Collective Hamiltonian (5DCH) [33] beyond-mean-field model with the Gogny DIS effective interaction [44, 45] to calculate energy levels of neutron-rich krypton isotopes and to investigate the weight of different deformations in the composition of their collective wave functions. Such features may be anticipated, based on topology displayed by the potential energy surfaces (PESs) which show deformed oblate and prolate minima separated by triaxial barriers \( \sim 2.1 \) and \( \sim 1.6 \) MeV high for \(^{98}\)Kr and \(^{100}\)Kr, respectively. Note that the 5DCH model successfully described the shape transition from an oblate ground-state in \(^{72}\)Kr to prolate in \(^{76}\)Kr and re-
revealed the key role played by the triaxial degree of freedom [46].

In Fig. 3, the calculated levels for $^{98,100}$Kr are compared to experiment. For both nuclei, the predicted ground-state band levels are in very good agreement with experiment (differences within 60 keV). More importantly, two excited levels $0^{+}_2$ and $2^{+}_1$ are predicted to lie between the $2^{+}_1$ and $4^{+}_1$ states. Our observation of a $(0^{+}_2, 2^{+}_1)$ state in $^{98}$Kr at 545(17) keV matches well with this prediction. 5DCH probability densities in the $\beta$ and $\gamma$ quadrupole deformation coordinate space are plotted in Fig. 4 for the $0^{+}_1$, $2^{+}_1$, $4^{+}_1$, $0^{+}_2$ and $2^{+}_2$ states. As shown in this figure for $^{98}$Kr, the yrast band is predicted to start from triaxial-oblate dominant $0^{+}_2$ and $2^{+}_1$ collective wave functions, evolving toward a stabilized prolate profile in the $4^{+}_1$ and higher-spin states (not shown). For $^{100}$Kr, the same transition is foreseen already from the $2^{+}_1$ state. Such an oblate to prolate shape evolution inside a band structure closely resembles those studied on the proton-rich side in $^{72}$Kr [47] and $^{70,72}$Se [48]. Furthermore, the $0^{+}_2$ and $2^{+}_2$ excited states intruding below the $4^{+}_1$ state in $^{98}$Kr are predicted to originate from a prolate shape competing at low energy with that for the oblate ground state as illustrated in top panel of Fig. 4. The shape-coexistent $0^{+}_2$ state persists at $N = 64$ in $^{100}$Kr but the $2^{+}_2$ state becomes even more triaxially spread with a collective wave function dominated by a $K = 2$ projected angular momentum component. More quantitatively, our calculations point to a rather smooth shape evolution starting in $^{96}$Kr and going to $^{100}$Kr, reflected by: (i) the progressive sign inversion of spectroscopic electric-quadrupole moments ($Q_{ep}$) from +20 to -62 $e\cdot fm^2$ for the $2^{+}_1$ state and from -49 to +27 $e\cdot fm^2$ for the $2^{+}_2$ state and (ii) the large inter-band $B(E2; 0^{+}_2 \rightarrow 2^{+}_1)$ values reaching 1653 and 2637 $e^2\cdot fm^4$ in $^{98}$Kr and $^{100}$Kr, respectively, and (iii) a significant mixing of angular momentum projected components ($K = 0$ and $K = 2$) in the $2^{+}$ states collective wave-functions. Going back to the krypton isotopic chain from $N = 56$ to 64 shown in Fig. 5, the calculated $E(2^{+}_1)$ energy trend shows a smooth and moderate decrease, in overall good agreement with experimental data. The marked energy decrease observed at $N = 62$ in the experiment is somewhat smoothed in the calculations as also noticed for Sr and Zr isotopes [33], a feature attributed to the lack of projection on good particle number in the 5DCH theory. Concerning non-yrast state, the $0^{+}_2$ state is predicted to dive in energy continuously from $N = 54$ to 60 and faster than the $2^{+}_1$ state, so that both states lie significantly below the $4^{+}_1$ state at $N = 62$.

To further investigate the robustness of our theoretical interpretation, we performed another beyond-mean-field calculation also using the Gogny D1S interaction but based on a symmetry-conserving configuration-mixing method (SCCM) as described in [34]. This approach relies upon the Generator Coordinate Method in ($\beta, \gamma$) variables within a space spanned by projected HFB states at good angular momentum and particle number. The level schemes obtained are also displayed in Fig. 3 for $^{98,100}$Kr. Agreement with experimental level energies similar to that achieved in the 5DCH approach is reached and a clear oblate-prolate shape coexistence situation is
also predicted, with a $0^+_2$ state calculated at 598 keV in $^{98}$Kr close to the 545(17)-keV experimental value. Both calculations and experimental data indicate that shape coexistence might drive the evolution of low-lying states in neutron-rich krypton isotopes. Still, differences on configuration mixing exists between the two models considered and a dedicated benchmark study in the spirit of those performed for neutron-deficient krypton isotopes [49, 50] would be relevant. For example, the SCCM calculations predict coexisting bands in $^{98}$Kr with very little mixing quantified by an inter-band $B(E2, 0^+_2 \rightarrow 2^+_1)$ value of only 19 e$^2$fm$^4$. It also predicts larger axial deformation in general and a sharp shape transition between $N = 62$ and 64, with a crossing in energy of the two coexisting configurations characterized by $Q_{sp}(2^+_1)$ going from +72 to -83 e·fm$^2$ for $^{98}$Kr and $^{100}$Kr, respectively.

Finally, relative γ-ray intensities with respect to the $2^+_1 \rightarrow 0^+_1$ transition indicate that the $^{99}$Rb(p,2p) reaction significantly populates the $(0^+_2, 2^+_2)$ state in $^{98}$Kr (I(216) > 50%). Based on recent studies of odd-even rubidium isotopes [51, 52] for $N \geq 60$, the ground states of $^{97,99,101}$Rb are understood as coming from a $\pi g_{9/2}/[431]3/2^+$ Nilsson-model configuration with a large prolate deformation. The selectivity of the (p,2p) reaction indicates thus a significant overlap between the $(0^+_2, 2^+_2)$ state in $^{98}$Kr and the prolate-deformed ground state of $^{99}$Rb, consistent with calculations. The non-observation of such a $(0^+_2, 2^+_2)$ state in the same energy range in $^{100}$Kr (< 40% of I(216) → 0$^+_1$) at a 95% confidence level) may indicate a change in the structure of low-lying non-yrast states with respect to $^{98}$Kr, requiring further experimental investigations.

To conclude, we performed the first spectroscopy of krypton isotopes beyond $N = 60$ and showed a significant drop of E(2$^+_1$) for $^{98}$Kr further stabilized for $^{100}$Kr. In $^{98}$Kr, the additional identification of a $(0^+_2, 2^+_2)$ state only 216(10) keV above the $2^+_1$ state provides the first experimental evidence of the lowering of an excited band coexisting with the ground-state one. Beyond mean-field calculations reproduce rather well the extracted energy levels and link them to the coexistence of oblate and prolate configurations competing at low energy, that might cross around $^{98,100}$Kr. These observations moderate the previously established picture of neutron-rich krypton isotopes as a sharp low-Z limit for the shape transition region at $N \simeq 60$ close to $A = 100$, and highlight that the richness of collective behaviors observed for neutron-rich zirconium and strontium isotopes extends to krypton.

This new step towards a delineation of the transitional region calls for the search of excited bands in $^{94,96}$Kr to further benchmark shape evolution scenarios, since extracting intra- and inter-band transition probabilities via Coulomb excitation of $^{98,100}$Kr still represents a longer term goal presumably requiring next-generation facilities.

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Note added: While this work was under review, the energy of the 4$^+_1$ state in $^{96}$Kr was measured in [53]. The corresponding data point has been added to Fig. 5 in this letter after the review process. Note that for $^{98}$Kr, our tentative (4$^+_1$) state at 827(20) keV leads to a $R_{42} = E(4^+_1)/E(2^+_1)$ of 2.51(8) significantly higher than the value of 2.12(1) obtained for $^{96}$Kr [53].

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