Germanium-gated $\gamma-\gamma$ fast timing of excited states in fission fragments using the EXILL&FATIMA spectrometer


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A B S T R A C T

A high-granularity mixed spectrometer consisting of high-resolution Ge and very fast LaBr$_3$(Ce)-scintillator detectors has been installed around a fission target at the cold-neutron guide PF1B of the high-flux reactor of the Institut Laue–Langevin. Lifetimes of excited states in the range of 10 ps to 10 ns can be measured in around 100 exotic neutron-rich fission fragments using Ge-gated LaBr$_3$(Ce)–LaBr$_3$(Ce) or Ge–Ge–LaBr$_3$(Ce)–LaBr$_3$(Ce) coincidences. We report on various characteristics of the EXILL&FATIMA spectrometer for the energy range of 40 keV up to 6.8 MeV and present results of ps-lifetime test measurements in a fission fragment. The results are discussed with respect to possible systematic errors induced by background contributions.

Keywords:
Fast-timing arrays
LaBr$_3$(Ce) scintillators
Lifetime measurements
The GCD method
Neutron capture gamma rays
Neutron induced fission

1. Introduction

Low-energy fission of trans-actinide nuclei produces neutron-rich, secondary fragments in the mass 80 < A < 160 region, often in conditions suitable for spectroscopic studies using large arrays of Ge detectors [1]. This reaction gives access to a wide range of nuclei difficult to study using conventional stable-beam accelerators and fusion reactions. The nuclei of this region exhibit a number of interesting nuclear-structure phenomena. For example, low-lying states of the several Z = 40 isotopic chains in the neutron-rich A = 100 region change shape from a spherical one at neutron number N = 58 to a strongly prolate-deformed one at N = 60 [2]. Evidence of shape coexistence in the nuclei here has also been presented [3,4], offering the opportunity to investigate the roles played by different orbits in the onset of quadrupole deformation. This region lies close to the light peak of the double-humped fission distribution.

The nuclei $^{78}$Ni and $^{132}$Sn are doubly magic in the spin–orbit coupling scheme. Fission can populate isotopes just a few nucleons

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away from $^{78}$Ni reasonably well. The immediate region around $^{132}$Sn lies almost at the heavy-wing peak of the fission distribution. Level schemes and lifetimes obtained from spectroscopic studies in these two regions can be compared to the predictions of shell-model calculations. The evolution of nucleon–nucleon interactions and the monopole migration of effective single-particle energies in neutron-rich regions are currently subjects of much interest in nuclear-structure studies. Measurements of the lifetimes of excited states can allow precise tests of shell-model predictions, probing the different orbit occupancies of states connected by a transition. In deformed regions lifetime information explores the degree of collective behavior present in a particular state.

Previously, lifetimes of excited states in fission fragments have been measured using several methods. These include direct-timing methods, following $\beta$ decay [5,6], though this is generally limited to studies of low-spin states. The fission reaction populates intermediate-spin states and lifetimes of these levels, and the ones below, have been determined using direct-timing methods with Ge detectors [7]. The poor timing performance of Ge detectors generally limits measurements of this type to lifetimes upwards of a ns. The characteristic Doppler broadening of $\gamma$ rays emitted by fission fragments slowing down in a thick backing has been used to obtain lifetimes of intermediate-spin states in the ps range [8]. Differential plunger experiments have also been used with spontaneous-fission sources, to obtain lifetimes in the ps-to-ns regime [9,10]. Measurements must be performed at some $10^8/(s cm^2)$ the number of events up to the same number of data sets. The $\gamma$ rays emitted from fission fragments in plunger experiments have three different energies, dependent upon the velocity of the fragment at the time they were emitted (fully shifted, partially shifted and stopped). The two $\gamma$-ray peaks emanating from in-flight decay are also Doppler broadened. Together all these effects result in complex spectra, limiting the technique for studies of fission fragments close to the peak of the fission–fragment mass distribution.

In the present article a description of the first prompt-fission $\gamma$-ray spectroscopy experiment, performed using a mixed array of Ge and Ce-doped LaBr$_3$, detectors, is presented. These detectors were placed around thin $^{235}$U and $^{241}$Pu targets, with thick backings, meaning that the fragments stopped in $\sim 1$ ps. Fission was induced by cold-neutrons from the collimated neutron guide PF1B [11,12] of the reactor of the Institut Laue-Langevin (ILL). Prompt $\gamma$-ray cascades from the nuclei of interest are selected via Ge- and Ce-doped LaBr$_3$ detectors, is presented. These detectors were installed on both sides of the central ring with detector angles of 40° and 140° relative to the beam direction. In order to provide the highest possible $\gamma-\gamma$ coincidence efficiency, the faces of the cylindrical LaBr$_3$ crystals with diameter of 1.5 cm were placed at 8.5 cm relative to the target position and were almost touching each other. The LaBr$_3$ crystals differ only slightly in their length; 8 crystals have a length of 1.5 cm while the other 8 crystals are 2 in. long. All LaBr$_3$ detectors utilise the Hamamatsu R9779 photomultiplier tube (PMT) which has superior energy and timing performance compared to previously used PMTs [14].

In order to provide the best fast-timing-array (FATIMA) time resolution power an analogue electronic “fast-timing” circuit as described in Ref. [15] was installed, consisting of constant fraction discriminators (CFD) of a single type (Ortec 935), multi channel logic fan-in/fan-out modules (FAN) and time-to-amplitude converters (TAC). This electronic set-up ensures that the TAC number $N_i = \lfloor \frac{\tau}{\tau_{i,j}} \rfloor$ of the $N$ detector timing system can only be started by detector number $i$ and stopped by a detector number $j \in [i+1, N]$. Each time peak $TAC_{i,j}$ of the $N(N-1)/2$ detector combinations $(i,j)$ with $i < j$ was individually adjusted approximately in the middle of the 50 ns-range TAC spectrum, by adjusting the cable length between the connections of the CFDs, FANs and TACs. This is made in order to allow the measurement of lifetimes up to 10 ns independent of the detectors hit and also to provide the best LaBr$_3$-LaBr$_3$ coincidence resolving time. Synchronised CAEN V1724 100 MHz digitizers were used to process and collect the energy signals of the LaBr$_3$, Ge and BGO detectors and the height of the TAC signals. Each signal is converted into an event which is stored trigger-less in a triple list-mode including (composite detectors, each made of 4 Ge crystals) with a target-to-detector distance of 14.5 cm. As illustrated in Fig. 1, two rings consisting of eight 5% Ce-doped LaBr$_3$ detectors each were installed on both sides of the central ring with detector angles of 40° and 140° relative to the beam direction. In order to provide the highest possible $\gamma-\gamma$ coincidence efficiency, the faces of the cylindrical LaBr$_3$ crystals with diameter of 1.5 cm were placed at 8.5 cm relative to the target position and were almost touching each other. The LaBr$_3$ crystals differ only slightly in their length; 8 crystals have a length of 1.5 cm while the other 8 crystals are 2 in. long. All LaBr$_3$ detectors utilise the Hamamatsu R9779 photomultiplier tube (PMT) which has superior energy and timing performance compared to previously used PMTs [14].

2. Set-up and performance of the EXILL&FATIMA spectrometer

2.1. Set-up

The basis of the experimental set-up is part of the EXOGAM array [13]. The central ring of the EXILL (acronym for EXOGAM at ILL) array around the target orthogonal to the beam direction has been equipped with 8 BGO-shielded EXOGAM clover detectors

![Fig. 1: CAD design of the EXILL&FATIMA spectrometer equipped with (a) BGO-shielded EXOGAM Ge-clover detectors and (b) LaBr$_3$(Ce)-scintillator detectors. Note the 3-dimensional central symmetry of the LaBr$_3$(Ce)-detector array with respect to the target position indicated with a +. The PF1B cold-neutron guide provides a halo-free neutron beam 12 mm in diameter with a high neutron flux of about $10^{10}/(s \cdot cm^2)$ at the target position [12].](image)
the ID of the channel, its amplitude and the time of registration (10 ns timestamp) using the digital pulse-shape algorithm described in Ref. [16]. To make this possible, the very fast LaBr3 energy signals (PMT dynode output pulse with decay time of about 2 ns) had to be shaped using RC-voltage of about 1 V per MeV. Fig. 3 presents the two extreme LaBr3 detectors energy responses of the FATIMA set-up, as obtained using data from the 48Ti(n,p)49Ti reaction. Up to 3 MeV corresponding to a PMT-anode amplitude of –3 V, the FATIMA-LaBr3 detectors have about the same, nearly linear, energy response. Above 3 MeV, the energy response becomes non-linear dependent on the detector. The non-linearity above 3 MeV is however relatively weak. The relative FATIMA energy resolution as a function of the energy, presented in Fig. 4, was obtained from the full width at half maximum (FWHM) of full-energy peaks in the spectrum of the superposition of the 16 calibrated LaBr3 spectra as shown in Fig. 2. The solid curve shown in Fig. 4 represents the ideal relative energy resolution as obtained for a linear energy response [18]. At the 137Cs energy of 662 keV, the relative energy resolution of the FATIMA set-up is 3.3%.

2.4. Full-energy peak efficiencies

A 152Eu point-like γ-ray source with activity of 362 kBq was used to measure absolute efficiencies in the energy region of 122–1408 keV. For the high energy region (787–6.1 MeV), the reaction 35Cl(n,γ)36Cl was used and relative efficiencies were

![Fig. 2. Semi-logarithmic plots of superimposed calibrated spectra representing the EXILL-Ge and FATIMA-LaBr3(Ce) singles γ-ray energy spectra of calibration measurements using (a) a 152Eu γ-ray source and (b) the in-beam reaction 48Ti(n,γ)49Ti.](image)
Table 1

<table>
<thead>
<tr>
<th>Detector (array)</th>
<th>$\epsilon_{122}$ (%)</th>
<th>$\epsilon_{662}$ (%)</th>
<th>$\epsilon_{1333}$ (%)</th>
<th>$\epsilon_{6111}$ (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>FATIMA</td>
<td>11.31(6)</td>
<td>3.71(7)</td>
<td>2.05(6)</td>
<td>0.38(10)</td>
</tr>
<tr>
<td>EXILL</td>
<td>12.58(6)</td>
<td>4.92(5)</td>
<td>2.97(4)</td>
<td>0.78(8)</td>
</tr>
<tr>
<td>EXILL$^a$+add-back</td>
<td>13.01(6)</td>
<td>5.80(5)</td>
<td>3.81(5)</td>
<td>1.22(11)</td>
</tr>
<tr>
<td>Ge crystal at 14.5 cm</td>
<td>0.41(1)</td>
<td>0.15(6)</td>
<td>0.093(3)</td>
<td>0.024(1)</td>
</tr>
<tr>
<td>1.5 in. long LaBr$_3$ at 8.5 cm</td>
<td>0.71(1)</td>
<td>0.21(1)</td>
<td>0.109(5)</td>
<td>0.020(6)</td>
</tr>
<tr>
<td>2 in. long LaBr$_3$ at 8.5 cm</td>
<td>0.70(1)</td>
<td>0.25(1)</td>
<td>0.145(6)</td>
<td>0.028(7)</td>
</tr>
</tbody>
</table>

$^a$ EXILL configuration with 32 Ge crystals in combination with FATIMA.

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2.5. Background considerations

Typical background obtained in γ-ray spectroscopy is most unwelcome in fast-timing experiments using γ rays. Considering energies larger than 300 keV, the background underneath the full-energy peak consists predominantly of Compton-scattered events. In this case, a Compton-timing correction for lifetime determination using a straightforward procedure can be performed, as will be demonstrated in Section 3. However, any correction procedure introduces additional errors which in turn reduce the accuracy of the lifetime determination. Below 300 keV, the Compton background becomes important when many γ rays are produced, as it then results from the superposition of many Compton continua of γ rays of higher energies. In addition, scattered γ rays can contaminate the γ-ray spectrum, in particular the back-scatter peaks around 200 keV. Such scattered γ-ray events are produced by a Compton scattering of an initial γ ray in the surrounding material of the set-up including the other detectors and the Compton-scattered γ ray then is detected. An active Compton suppression, for instance by using BGO scintillators, also acts as an active shield for LaBr$_3$ detectors, reducing remarkably events resulting from scattered γ rays [20]. A simple estimate of the solid angle indicates that the LaBr$_3$–LaBr$_3$ coincidence efficiency would drop by a factor of 2 if the distance of the LaBr$_3$ detectors was increased by only 2 cm, the distance necessary to install efficient shielding. Therefore, we dispensed with the use of any active or passive LaBr$_3$-detector shielding.

We performed an investigation of the possible effect of scattered γ rays by generating gated spectra of pure LaBr$_3$–LaBr$_3$ double events (γ-ray multiplicity equal to 2) for different detector combinations ($i$,$j$) with $j > i$, as illustrated in Fig. 6. By combining an LaBr$_3$ detector located on one side of the central EXOGAM-clover ring with an LaBr$_3$ detector located on the opposite side of the central ring [e.g. for combination (1,9)] the expected gated LaBr$_3$ coincidence spectrum with almost Gaussian shaped full-energy peaks is observed. The corresponding LaBr$_3$ coincidence spectrum (a) of Fig. 6 was generated by using an LaBr$_3$ gate on the 444-keV transition in $^{152}$Sm, as obtained using the $^{152}$Eu source. Note also the almost constant Compton continuum of the 964-keV transition and the constant increase of the Compton background for energies below the other full-energy peaks. $^{152}$Eu partially decays to excited states in $^{152}$Sm via electron-capture decay.

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Fig. 4. The LaBr$_3$(Ce)-FATIMA relative energy resolution corresponding to FWHM/$E_\gamma$. The calibration function is proportional to $1/\sqrt{\alpha+E_\gamma}$ with $\alpha$ being related to the PMT gain variance [18].

Fig. 5. The absolute full-energy peak efficiency curves of (a) the FATIMA set-up, (b) the EXILL array and (c) the EXILL array including add-back algorithm.

Fig. 6. The effect of cross-talk events [spectrum (b)]: The LaBr$_3$(Ce) detector number 1 coincidence spectra obtained with a gate on the 444-keV transition in $^{152}$Sm using (a) a non-neighbouring LaBr$_3$(Ce) detector and (b) a directly neighbouring LaBr$_3$(Ce) detector. Spectrum (c) is the singles energy spectrum as obtained using the $^{152}$Eu source, that is shifted by $-444$ keV for comparison.
(72.1% [21]) and states in $^{152}$Gd via $\beta^-$ decay. The 444-keV transition in $^{152}$Sm is a doublet with coincident transitions of 122, 244, 964 and 1085 keV. The $^{152}$Gd peak at 344 keV is due to accidental coincidences with the Compton background underneath the 444-keV peak (see also Fig. 2a). Unsurprisingly, the central EXOGAM-clover ring serves as an effective passive shield. The dramatic effect of scattered $\gamma$ rays coming from directly neighbouring LaBr$_3$ detectors is illustrated by spectrum (b) of Fig. 6. Using the same LaBr$_3$ gate at 444 keV, the resulting coincidence spectrum of the directly neighbouring LaBr$_3$ detector is full of “ghost peaks” which are overlapping with the transitions of interest. By comparing spectrum (b) with spectrum (c), the superimposed structure seen in spectrum (b) corresponds to the singles energy spectrum of the $^{152}$Eu source which is shifted by exactly – 444 keV, corresponding to the energy of the LaBr$_3$ gate. This clearly indicates that an initial $\gamma$ ray depositing energy from a Compton-scattered event in one detector and the Compton-escaped $\gamma$ ray being absorbed by the neighbouring detector. This therefore provides a false $\gamma-\gamma$ coincidence, often called a “cross-talk event” with a false timing information related to the time-of-flight of the Compton-scattered $\gamma$ ray. Fortunately, such undesired cross-talk events are only observed in adjacent LaBr$_3$-detector combinations. The detector combinations ($ij$) with $j > i + 1$ all show identical clean coincidence spectra as the spectrum (a) as shown in Fig. 6. One can say that the combinations ($ij$) with $j > i + 1$ within a ring are passively shielded by the detectors $i + 1$. While add-back is straightforward, there is no simple algorithm that could take into account the time information of the initial $\gamma$ ray, since corrections would introduce additional errors. Instead, we refrained from using detector combinations ($ij$) with $j = i + 1$ within the LaBr$_3$ rings for further analysis. In this way, the excluded detector combinations ($ij$) with $j = i + 1$ partially act as an active shield for combinations with $j > i + 2$ and thus also the Compton background in both LaBr$_3$ spectra $i$ and $j > i + 2$ is reduced. In total, 16 detector combinations out of 120 are excluded from the analysis, corresponding to a relative loss of about 13% in statistics.

An advantage of fast timing with LaBr$_3$(Ce)-scintillator detectors is that they offer good energy resolution allowing for clean selection of $\gamma$ lines. Still, when the $\gamma$-ray spectrum is complex such as those in our experiments, the energy resolution may not be sufficient to disentangle the transition of interest amidst other $\gamma$ lines. Our experiment has been specifically designed to allow for cascade selection by exploiting the high-resolution Ge detectors of the EXILL array. In this way, a $\gamma$ ray of a subsequent triple-$\gamma$ cascade is selected as a trigger [22]. Beside the possible exclusion of unwanted contaminating $\gamma$ rays from other cascades or nuclei, this procedure improves the peak-to-background ratio remarkably due to suppression of most of the $\gamma$ rays that are shown in the singles spectra, as can be seen in Fig. 7. The higher the energy of the EXILL triggering transition, the more effective is the Compton-background reduction observed in the doubly gated (Ge + LaBr$_3$) LaBr$_3$ coincidence spectra. In a de-excitation pattern with multiplicity 3, the resulting doubly gated LaBr$_3$ spectrum often shows the spectrum of a single $\gamma$ ray with virtually no Compton background, as shown in Fig. 7.

### 2.6. $\gamma-\gamma$ timing performance of FATIMA

To be able to exploit lifetimes down to values corresponding to the intrinsic timing resolution of any $\gamma-\gamma$ fast-timing set-up, the time response of the set-up as a function of the energy of prompt $\gamma-\gamma$ cascades, or “prompt response functions” (PRF), needs to be determined. The time response, defined by the centroid of the PRF, represents the zero-time $t_0$ relative to the physical prompt reference and needs to be measured using different $\gamma-\gamma$ cascades.

$$\delta t = \frac{\text{FWHM}}{2 \sqrt{2 \ln 2}} \approx 1 \text{ ps}$$

(1)

where $n$ is the number of events of which the PRF is built up. Assuming no background contributions, a “delayed” time spectrum is measured as the convolution of the PRF $P(t)$ with an arbitrary decay [23]:

$$D(t) = \int_{-\infty}^{\infty} P(t - t_0)e^{-\lambda(t-t_0)}dt$$

(2)

where $\lambda$ is the transition probability and $\tau$ is the mean lifetime of the nuclear excited state interconnected by the $\gamma-\gamma$ cascade and $t_0$ is the centroid of the PRF. For lifetimes which are larger than the FWHM of the PRF, the slope method is used by fitting the straight line observed in the semi-logarithmic plot of $D(t)$ outside the region of the PRF, as $\ln(D(t)) = -\lambda t$ for $t \gg t_0$. The slope method is independent of the shape of the PRF [23].

Assuming no background contributions, the method to measure lifetimes with highest precision is the centroid-shift method [24]. The centroid or centre of gravity is the first moment of the statistical distribution and for an arbitrary time spectrum $D(t)$ is defined as

$$C^0 = \langle t \rangle = \int_{-\infty}^{\infty} D(t) dt \frac{dD}{dt} \sigma C^0 = \sqrt{\langle t^2 \rangle - \langle t \rangle^2}$$

(3)

For a symmetric Gaussian PRF, the statistical uncertainty of the centroid determination $\sigma C^0$ is equal to $\delta t$ from Eq. (1). Basically and assuming no background contributions, the mean lifetime directly corresponds to the relative time difference between the centroids of the delayed time spectrum and the energy corresponding PRF as [24]

$$\tau = \pm \left[ C^0 - C^0 \right]$$

(4)

where the sign is negative if the decay transition of the $\gamma-\gamma$ cascade provides the start signal to the TAC (“the anti-delayed time spectrum” [23]). As demonstrated experimentally in Refs. [25,26], the centroid-shift method is independent of the shape of the PRF.

Considering specific detector combinations, one generally observes small differences of the decisive FWHM of the PRF dependent on the detector combination. According to the Hyman
theory of timing [27], the time resolution of a scintillator plus PMT detector assembly is proportional to the figure of merit \( \sqrt{\tau_{\text{sc}}/N_{\text{pol}}} \), where \( \tau_{\text{sc}} \) is the scintillator decay time and \( N_{\text{pol}} \) is the number of photoelectrons produced at the photo cathode of the PMT by the scintillation light pulse. Thus, the timing is controlled by the scintillator light output and the PMT photo-cathode sensitivity [28,29]. Using large volume scintillators \( > \Phi 0.5 \text{ in.} \times 1.5 \text{ in.} \), the time spread of the scintillation light collection at the PMT photo cathode dominates over the PMT time jitter (transit time spread of photoelectrons) [30,31]. We measured the FWHM to be 210–240 ps when combining two "small" LaBr3 scintillators (\( \Phi 0.5 \text{ in.} \times 1.5 \text{ in.} \)) using a \( ^{60}\text{Co} \) source (1173–1333-keV cascade with \( \tau = 1.06(3) \text{ ps} \)) [32]. By combining two large scintillators (\( \Phi 0.5 \text{ in.} \times 2 \text{ in.} \)), the result is 260–300 ps. The small differences of the FWHM for combinations of equal volume detectors may be associated with a spread in the quality of the crystals due to variation of Ce doping [33]. Small variations of the CFD adjustments (CFD shaping delay, threshold and walk) can also slightly affect the FWHM [26]. An additional detector combination dependent electronic time jitter is given due to cable-length dependent degradation of the signal-to-noise ratio and the generation of additional noise by the individual electronic modules of the fast-timing circuitry [15]. The most important factor overall in this experiment is the FATIMA timing performance, which is obtained by a superposition of the \( N(N-1)/2 \) calibrated “TAC\textsubscript{\( j,j' \})” time spectra. To provide the best FATIMA timing performance, only an alignment of the calibrated TAC\textsubscript{\( j,j' \}) spectra needs to be applied to the raw data by using error-free constant-shift values “\( \text{shift}\textsubscript{\( j,j' \}) \)” (implemented in SOCOv2 [17]). The precise \( \text{shift}\textsubscript{\( j,j' \}) \) constants were derived from the measurement of the “stop” centroid \( C_{\text{stop}} \) of each single TAC\textsubscript{\( j,j' \}) time spectrum of a specific \( \gamma-\gamma \) cascade. The FATIMA PRFs presented in Fig. 8 represent the TAC-aligned and superimposed FATIMA “stop” time spectra as obtained when the decay transition was registered by detectors which provided the stop signals to the TACs of the set-up.

As a result of statistical processes in the creation of the detector output pulse, the FWHM of the PRF is dependent on the \( \gamma \)-ray energy of both the feeding (start signal) and the decaying (stop signal) transitions. The main component is induced when the signals have smaller amplitude (energy), as the relative amplitude variation (jitter) increases with decreasing amplitudes [35]. At very high energies, as the case presented in Fig. 8b, the relative amplitude variation is marginal and the FWHM is dominated by the crystal-size dependent time spread of the scintillation light collection. For energies larger than 1.2 MeV, the FWHM of the combined FATIMA PRF is 270(20) ps. The energy dependent FATIMA timing performance is presented in Fig. 9, where the data are fitted using a function \( \Delta T(E) \) which describes the CFD timing uncertainty and time walk according to [26,35]

\[
\Delta T(E) = \frac{a}{\sqrt{E+b}} + \text{pol}(E),
\]

where \( \text{pol}(E) \) is a polynomial of order \( n \). In our case, the best fit was obtained for \( \text{pol}(E) \) being a constant which is expected for a linear energy response [26]. According to Eq. (1) and assuming only 1000 events in a PRF with no background contribution, the statistical uncertainty of the PRF-centroid determination is less than 5 ps for energies larger than 300 keV.

In analogy to a simple two detector \( \gamma-\gamma \) timing system, it is very important to distinguish between the “start” and the “stop” time spectrum, as the electronic timing uncertainty (time-jitter) of the start and stop signals are, in general, different (the so-called “timing asymmetry” [21]) and provoke asymmetric semi-Gaussian prompt time spectra (PRFs). As illustrated in Fig. 10a, neither the start and stop time spectra nor the shift of both time spectra relative to the reference zero-time are mirror symmetric. In this case, the timing asymmetry arises from the disparities of the individual detector time responses (time walk) as a result of the different energy responses observed for large energy differences \( \Delta E_i = |E_{\text{order}} - E_{\text{decay}}| > 3 \text{ MeV} \) (see also Fig. 3). But in spite of this fact, the centroid difference, that is the time shift between the centroids of the stop and start time spectra for a specific \( \gamma-\gamma \) cascade, is independent of any timing asymmetry [15,26,36].
For any energy combination of a prompt possible to precisely calibrate the energy dependency of the PRD. The mirror symmetric centroid difference makes it a target of the GCD identity PRD points with the same uncertainty are obtained by taking advantage of the FWHM. Ref. [26]. The PRD curve of the FATIMA set-up, presented in Fig. 10, which also shows that the applied shift, \( \tau \), constants do not introduce systematic errors. While the centroid difference is unchanged for different constants, the precision of the measurement can be improved following Eq. (1) by minimising the FWHM.

The advantage of the generalised centroid difference (GCD) method is that the centroid difference is mirror symmetric [36]. By referring to the decay transition and according to Eq. (4), the following relation is strictly valid:

\[
\Delta C(\Delta E)_{\text{decay}} = C_{\text{stop}} - C_{\text{start}} = \text{PRD}(\Delta E)_{\text{decay}} + 2\tau
\]

with \( \Delta E = E_{\text{feeder}} - E_{\text{decay}} \). PRD = \( C_{\text{stop}} - C_{\text{start}} \) is the prompt response difference and represents the linearly combined \( \gamma - \gamma \) time response (time walk) of the complete fast-timing system (the measured PRD mathematically corresponds to the mean value PRD for \( N > 2 \) [15] and is hereafter not indicated). \( C_{\text{start}} \) is the centroid of the time spectrum which is obtained for the reference energy, the decay energy in Eq. (6), being the energy of the stop (start) gate. The mirror symmetric centroid difference makes it possible to precisely calibrate the energy dependency of the PRD. For any energy combination of a prompt \( \gamma - \gamma \) cascade, two data points with the same uncertainty are obtained by taking advantage of the GCD identity PRD(\( \Delta E \), 0) = 0. The two data points are transformed into the \( \Delta C(E, \gamma) \) representation according to [15,26]

\[
\text{PRD}(E_{\text{feeder}} - E_{\text{decay}}) = \text{PRD}(E_{\text{feeder}}) - \text{PRD}(E_{\text{decay}}).
\]

According to Eq. (6), also precisely known ps lifetimes can be used for the PRD-calibration procedure, as described in more detail in Ref. [26]. The PRD curve of the FATIMA set-up, presented in Fig. 11a, was obtained by adjusting the two data points of 16 \( \gamma - \gamma \) cascades in parallel to fit the smoothest PRD curve. Some 82% of the PRD data were obtained using triple events (multiplicty 3) with an additional EXILL gate which resulted in almost zero background contributions, as the case presented in Fig. 7. Triple \( \gamma - \gamma - \gamma \) events were used from a 40-hour measurement using a \( ^{152}\text{Eu} \) point like \( \gamma \)-ray source for the energy range of 40–1408 keV and from a 20-hour measurement using the \( ^{48}\text{Ti}(n_{\text{th}}, \gamma)^{50}\text{Ti} \) reaction for the energy range of 137–6760 keV. The rest of the PRD data are from double events, where \( \gamma - \gamma \) cascades were used which provided peak-to-background ratios larger than 20. No significant timing effects due to the background contributions were found in these cases. The PRD data are fitted by a function according to Eq. (5) with a second order polynomial. The quality of the PRD calibration is represented by the deviations of the data from the fit, as shown in Fig. 11b. By taking statistical uncertainties into account, an overall PRD uncertainty of 10 ps is achieved. No further error is given by this PRD-calibration procedure, as no corrections have been applied to the raw data. Although the metallic Ti target had a surface area of about 40 mm\(^2\), the results are consistent with the \( ^{152}\text{Eu} \) data in the overlapping energy region of 137–1408 keV.

Measurements have been performed to test the long-term stability of the set-up by means of two further 3-hour calibration of the PRD using the \( ^{152}\text{Eu} \) source. As illustrated in Fig. 12a, the 3 measurements were separated over the fast-timing campaign of 5 weeks. Compared with the PRD uncertainty of 10 ps, no significant change of the PRD characteristics in the low-energy region of 40–1408 keV can be observed. Additional PRDs were measured using an extended \( ^{60}\text{Co} \) source with a diameter of 10 mm and the superimposed data of several 1-hour high-energy-calibration measurements using double events from a
$^{35}$Cl$(n, \gamma)^{36}$Cl reaction for the almost prompt indirect 6111–1951-keV $\gamma$–$\gamma$ cascade. In the case presented in Fig. 12b, the effective lifetime obtained corresponds to $\tau_{\text{eff}} = \tau_1 + \tau_2$ [25]. If $\tau_1$ is known, $\tau_2$ can also be derived in this way, which can provide a more precise result when the spectrum of the direct feeding transition has a $\gamma$-ray contamination or has a bad peak-to-background ratio. Within statistical uncertainties, the results are consistent with Eq. (7) using the PRD curve presented in Fig. 11a. As the dimensions of the sources and targets were different and also their positions in the spectrometer to within about 2 mm, the results also indicate that the use of a 3-dimensional centrally symmetric FATIMA setup in combination with the GCD method reduces geometrical timing effects to an unmeasurable value in our case.

3. Tests on the $^{235}$U fission experiment

In $(\text{n}_{\text{th}}, \gamma)$ experiments, the use of a high-resolution energy gate using Ge detectors as a coincidence trigger provides a considerable Compton-background reduction which is important for $\gamma$–$\gamma$ fast-timing measurements. Owing to the low $\gamma$-ray multiplicity of these type of reactions, the doubly gated (Ge + LaBr$_3$) LaBr$_3$ coincidence spectrum often contains only one $\gamma$ ray, and virtually no background is underneath the full-energy peak, as illustrated in Fig. 7. If this is the case for both the feeding and the decay transitions, the resulting LaBr$_3$–LaBr$_3$ time spectrum is free of background. In the most general situation one has to deal with Compton-background contributions, and in particular in prompt fission experiments, where the $\gamma$-ray multiplicity is much higher and the amount of $\gamma$ lines is increased by a factor of 100 or more compared to relatively clean $(\text{n}_{\text{th}}, \gamma)$ experiments. By using two high-resolution Ge gates, a clean spectrum of one $\gamma$ line can be...
obtained, but at the expense of much reduced statistics, since the probability to record multiplicity 4 events is about 1–5% of the triple efficiency. Also the relative γ-ray intensity ratio within a selected quadruplet γ-ray cascade can be reduced.

For the purpose of investigating the timing effect of the Compton background, two results of the cold-neutron-induced fission experiment on 235U are presented. This experiment delivered the highest count rates during the EXILL&FATIMA campaign with about 10 kHz for a single Ge crystal and 15 kHz for an LaBr3 detector. A data rate of about 6.5 MB/s was created by the 71 channels of the EXILL&FATIMA spectrometer. The target consisted of 0.8 mg 235UO2 tightly sandwiched with cyanacrylate between two 15–μm thick Be backings in order to stop the neutron-induced fission fragments within the target. The analysis was performed using multiplicity 3 events out of 0.8 TB of data, corresponding to a tenth of the acquired data. The total projection of the EXILL array including add-back and BGO Compton suppression is shown in Fig. 13a. The transitions labelled belong to the nucleus 100Zr which has a fission yield of 4.98%, close to the maximum value. Fig. 13b shows the comparison of the EXILL and FATIMA projections of triple events generated by using a clover add-back gate on the 497-keV 6− → 4− transition. The two spectra show similar structures with expected strong peaks at 352 keV and 212 keV. Since the introduced Compton suppression of the LaBr3 detectors geometrically does not fully cover the LaBr3 crystals, the peak-to-background ratio of the FATIMA projection is slightly worse. The small peaks identified in the EXILL projection can be due to true coincidences, e.g. with a γ-ray from a state above the 6− state, or from a double γ-ray cascade in another nucleus. The doubly gated EXILL spectrum of the 352-keV 4− → 2− transition presented in Fig. 13c was obtained using a clover add-back gate on the 497-keV transition and a 10-keV-wide LaBr3 gate centred on the 212 keV 2− → 0− ground-state transition. This high-resolution spectrum allows investigations of possible coincident γ-rays in the vicinity of ± 20 keV, dependent on the energy range) of the 352-keV transition. A similar investigation of the 212-keV ground-state transition is shown in Fig. 13d. In both cases, no significant full-energy peak is observed in the vicinity of the transitions of interest using Ge-LaBr3 gated spectra of triple events. Thus the lifetime of the first 2− state can be measured using Ge-LaBr3-LaBr3 coincidences, and only Compton background will additionally contribute to the time spectra.

Fig. 14a shows a doubly gated FATIMA LaBr3 spectrum of the feeding transition at 352 keV (LaBr3 energy projection of the Ge-LaBr3 gated fast-timing matrix). A large Compton background is observed, the peak-to-background ratio as obtained for the energy width corresponding to the width of the LaBr3 gate is 2.5 (2). Thus about 40% of the counts in the EXILL-gated γ−γ time spectra shown in Fig. 14b are background events (e.g. full-energy vs. Compton and Compton vs. Compton). The two start and stop time spectra show a pronounced decay slope from which the lifetime can be extracted assuming the background time distribution to be nearly prompt. This assumption is safe, since the centroid difference is much smaller than 2τ; the PRD for the energy combination 352−212 keV is only −62(10) ps. The measurement by means of the slope method results to a mean lifetime of 720(40) ps.

To obtain the lifetime from the centroid shift, the time response or “timing” (centroid of time spectrum) of the background underneath the full-energy peak has to be taken into account, in order to perform the Compton-timing correction [6,25] to remove its contributions from the time spectrum as shown in Fig. 14b. Obviously, the time spectrum of the background events at 352 keV cannot be measured directly. However, the timing of the Compton background underneath the full-energy peak at 352 keV can be extrapolated precisely. The two (start and stop) fast-timing matrices allow for a quick background analysis by generating a set of time spectra using gates set in the Compton background around the full-energy peak. For proper time correction, the energy width of the Compton gates need to correspond to the width of the full-energy gate. The result of the Compton-background analysis on the 352-keV feeding transition is presented in Fig. 14c, where the indicated PRD curve PRD (Eγ) is adjusted for the reference energy of 212 keV (parallel shift of the PRD curve in order to cross the energy axis at 212 keV). The Compton-background events are largely delayed which is partially due to the lifetime of the
The lifetime using the centroid shift methods is derived as a linear combination of centroids, the measured centroid difference corresponds to [36]

$$\Delta C = \frac{\Pi \Delta C_{\text{true}} + \Delta C_{\text{Compton}}}{1 + \Pi}$$  \hspace{1cm} (8)

where $\Pi$ is the peak-to-background ratio and $\Delta C_{\text{true}}$ is the true centroid difference. It follows:

$$\Delta C_{\text{true}} = \Delta C + \frac{\Delta C - \Delta C_{\text{Compton}}}{\Pi}$$  \hspace{1cm} (9)

and thus

$$\tau_2^{-1} = \frac{1}{2} \left( \Delta C + \frac{\Delta C - \Delta C_{\text{Compton}}}{\Pi} - \text{PRD} \right) = 730(30) \text{ ps},$$  \hspace{1cm} (10)

which is in good agreement with the results obtained using the slope method (Fig. 14b). This result has been verified by an analogous Compton-background analysis on the 212-keV ground-state transition, thus with $E_{\text{eff}} = 352$ keV and EXILL triggering on the 497-keV $\gamma$ ray. Although the peak-to-background ratio and the time shift between the full-energy and Compton events at 212 keV are different than the reversed case presented in Fig. 14, the results after corresponding time correction are consistent within errors. This is expected when the full-energy peak of both the feeding and decaying $\gamma$ rays are sitting on Compton background [36]. Otherwise, it is important to investigate for the peak-to-background ratios of both $\gamma$ rays, as after multiple gating, the Compton background can be eliminated for certain energies and thus not necessarily for both $\gamma$-ray energies each completely.

A similar Compton-background analysis for the determination of the lifetime of the first $4^+$ state in $^{100}$Zr is presented in Fig. 15. In this case no significant difference in the timing of the full-energy and the Compton events can be observed at 497 keV. According to the peak-to-background ratio of $\Pi = 1.8(2)$ an additional error of 10 ps is taken into account for the determination of the centroid difference corresponding to the relative timing uncertainty of the Compton events. Thus the result here is $\tau_{4^+} = 42(8)$ ps. Although the large background may have a small contribution of the 511 keV annihilation $\gamma$-rays, the result obtained is in good agreement with the literature value indicated in Fig. 15b.

4. Conclusion

Large high-efficiency Ge and LaBr$_3$(Ce) detector arrays have been assembled and installed at the intense cold-neutron guide PF1B of the ILL. The EXILL/FATIMA spectrometer allows for the first time to perform fast-timing lifetime measurements in prompt $\gamma$-ray spectroscopy experiments on exotic neutron-rich fission fragments. Extensive calibration measurements have been performed to test the precision of such a high-granularity fast-timing array by using the mirror symmetric GCD method. This new approach delivers a new fast-timing-array spectrometer constant, namely the mean prompt response difference between the start
and stop events of the FATIMA set-up. Whereas the timing between single detector pairs is sensitive to the position and the extensions of the γ-ray emitter, the 3-dimensional centrally symmetric fast-timing array in combination with the GCD method is shown to largely cancel the geometrical timing effects. In addition, possible systematic errors due to the typical timing asymmetries and time drifts are also cancelled. Over 5 weeks of operation, no significant change of the prompt response difference curve has been detected. The prompt response difference was measured for the total dynamic range of the FATIMA set-up ranging from 40 keV up to 6.8 MeV with an overall precision of 10 ps. The fast-timing performance of the presented FATIMA set-up, given as the γ–γ coincidence FWHM of prompt time spectra, is 270–500 ps for energies larger than 100 keV. This allows to access lifetimes of nuclear excited states below 300 ps with precision better than 10 ps with only 1000–2000 Ge–LaBr3–LaBr3 or Ge–Ge–LaBr3–LaBr3 coincidences. Thanks to the high-efficiency EXILL array, around 100 neutron-rich isotopes with lifetimes larger than 0.1% will be investigated from the data sets acquired using 235U and 248Pu targets during the EXILL&FATIMA campaign in 2013.

Extensive studies on the influence of the background in γ–γ fast-timing experiments have been performed. Inter-detector Compton scattering has been shown to be important only for adjacent LaBr3–detector combinations. Such cross-talk γ–γ coincidences have been excluded from the analysis, resulting in a geometrical shielding for the other detector pairs, and thus a Compton suppression. Thanks to high-resolution gating using EXILL, the Compton background in the doubly gated (Ge+LaBr3) LaBr3 coincidence spectrum is remarkably reduced, even to negligible contributions in special cases. Otherwise, the proposed time-correction procedure related to the timing of the Compton background underneath the full-energy peak of interest has been shown to be accurate and reliable. For peak-to-background ratios larger than 2 and for about 2000 γ–γ events, the error of this time-correction procedure is smaller than 10 ps. In prompt fission-fragment experiments as proposed in this article, a better lifetime precision can be obtained using quadruple Ge–Ge–LaBr3–LaBr3 gates as thousands of γ rays produce massive Compton background that cannot be effectively reduced or even fully suppressed using only one EXILL gate. In any case, a range of gates are possible in the nucleus of interest and on some of the transitions in complementary fission fragments to increase the statistics.

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